



UNIVERSIDAD DE CHILE  
Facultad de Ciencias  
Físicas y Matemáticas



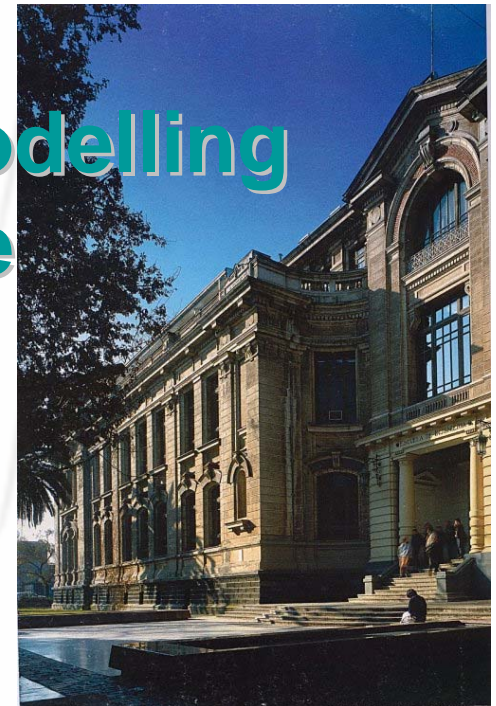
CENTRE NATIONAL  
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SCIENTIFIQUE

# Computing Optimal Equilibrium Strategies for Network Economies

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# Traffic Assignment Problem



## Basics

- One of the most basic problems in transportation research
- Every individual travel along the shortest available path (considering congestion)
- Formulated as an equilibrium or fixed point problem
- Deterministic or stochastic models
- Stochastic models are more realistic but need more computation.
- Actual stochastic models are computational impractical for large networks.



Some software:

emme/2



# Markovian Traffic Equilibrium

(Baillon, Cominetti, Math. Programming, to appear)



## Details

- Based on discrete choice models but imbedded in a dynamic programming framework.
- At every intermediate node it selects the next street in a route to the destination, recursively.
- It take into account the variability of user preferences, stochastic congestion and uncertain travel times.
- It assume a randomness in the traffic of an arc, constructing a Markov chain.
- Model characterized with an unconstrained, strictly convex and coercive formulation, implying the existence and uniqueness of the solution.
- It avoids path enumeration, allowing to compute large networks.

Para ver esta película, debe  
disponer de QuickTime™ y de  
un descompresor YUV420 codec.

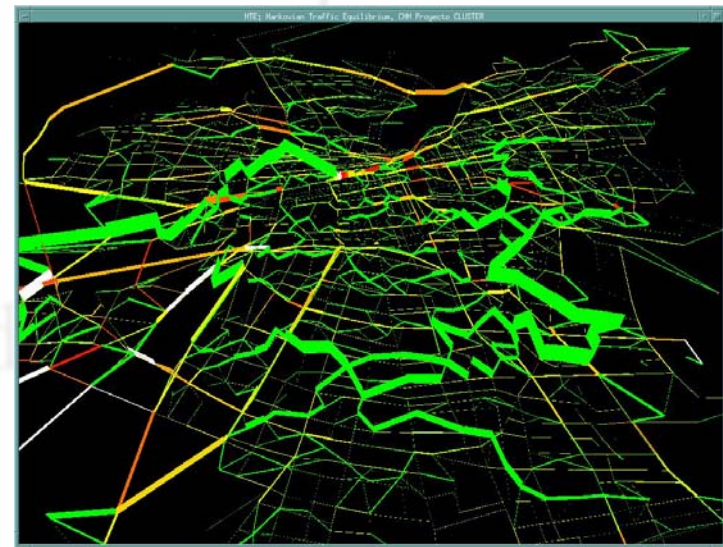
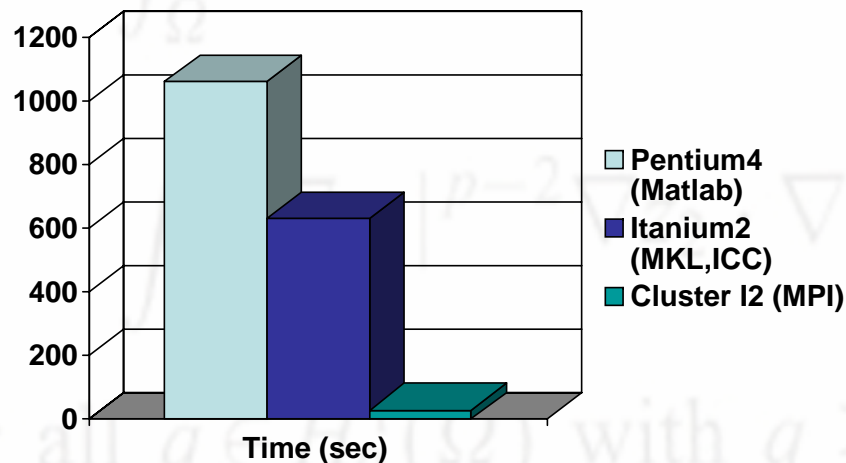
# MTE: Practical Issues



- Code originally written in Matlab
- Code rewritten in C using Intel MKL Libraries (VML, BLAS, PARDISO)
- Tuned for Intel Itanium 2 (but portable to other architectures)
- Parallelized using MPI Library

## Computation Time

Chicago Network (546 destinations, 2176 streets)



Santiago network (2159 destinations, 7587 streets)

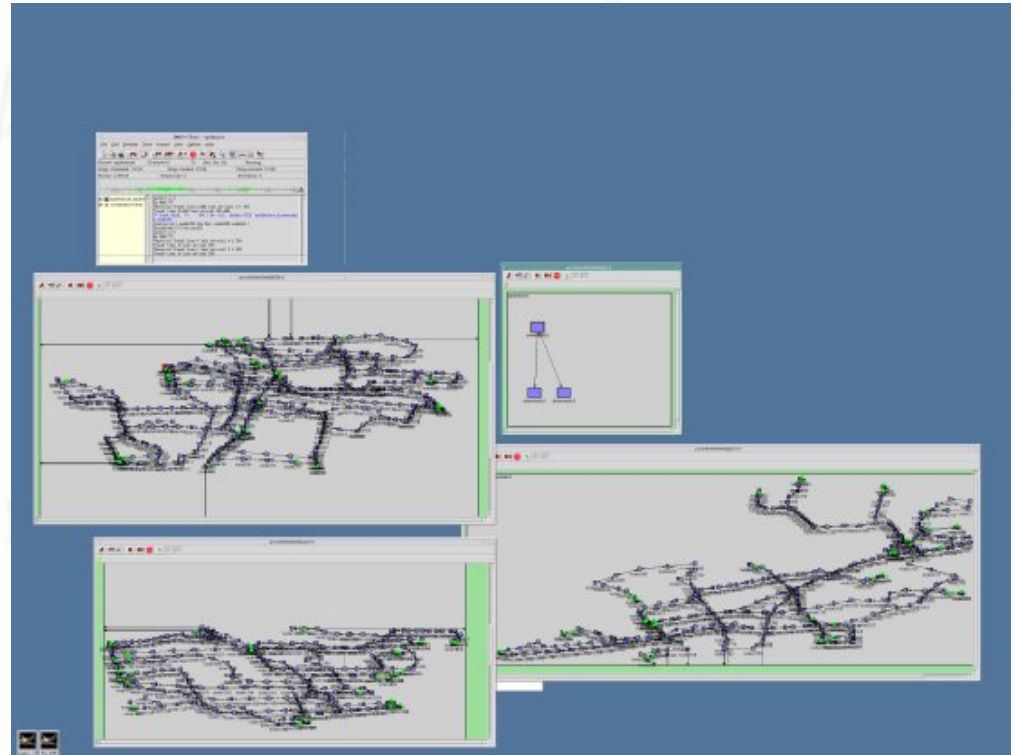


# Parallel Discrete Event Simulation: Public Transportation System



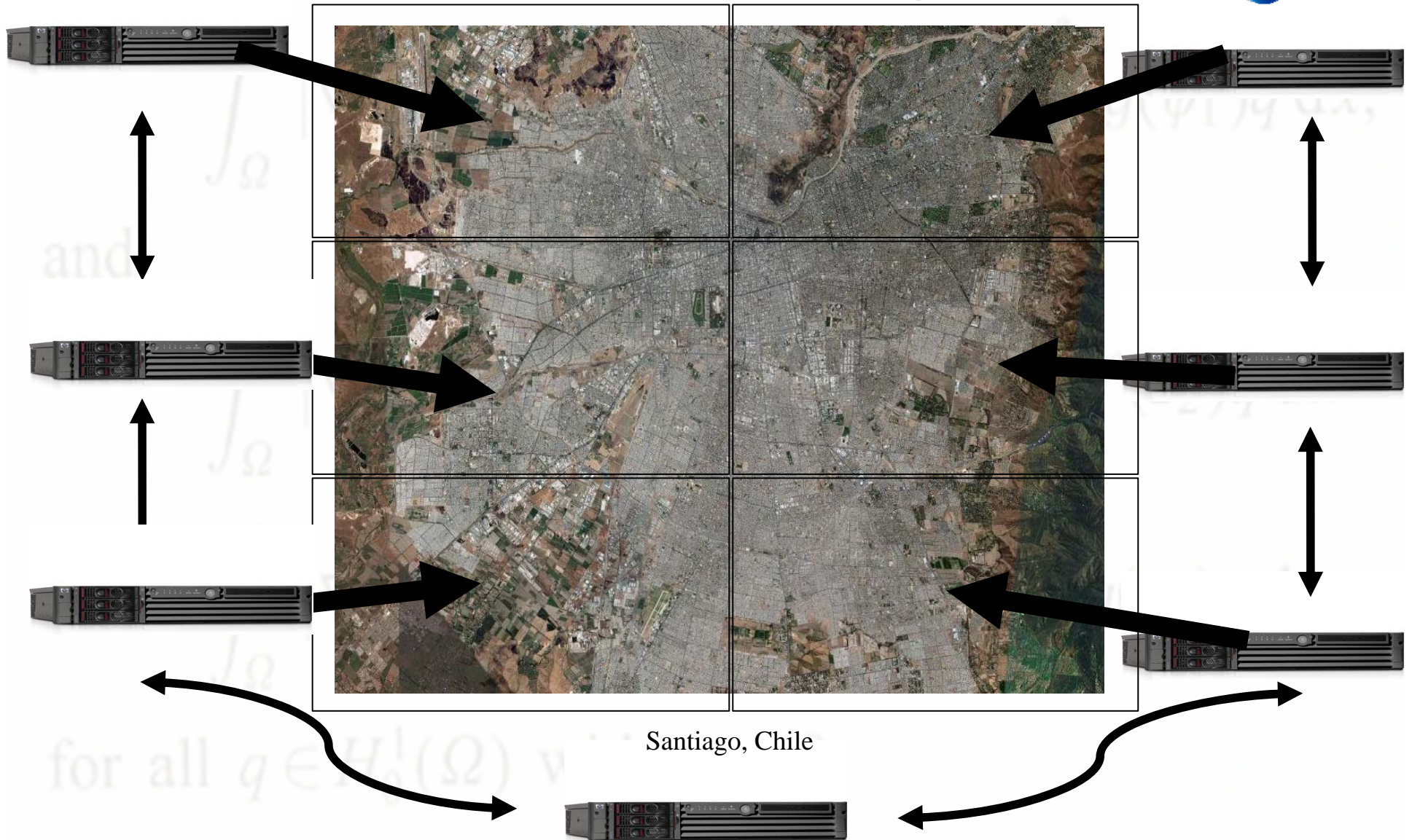
## Keywords:

- Large transit networks
- Congestion
- Passenger perception
- Discrete event simulation
- Object oriented simulation
- Clustered databases
- MPI Communications



This model attempt to provide a simulated public transport scenario that can be use to improve the manager decisions respecting to public transportation policies. It analyzes a Wardrop equilibrium model for passenger assignment in general transit networks, including the effects of congestion over the passengers' choices.

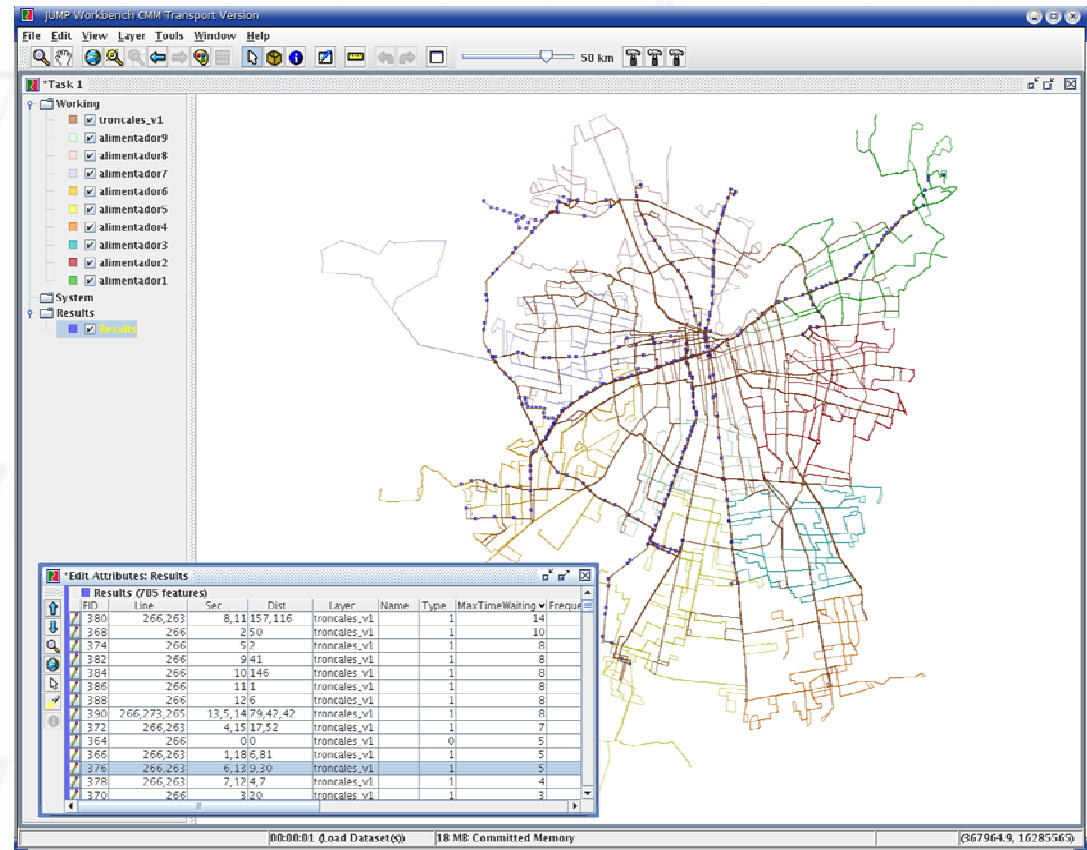
# Parallel Discrete Event Simulation: Public Transportation System



# Parallel Discrete Event Simulation: Public Transportation System



The model engine that runs on the cluster feeds on-line a graphical interface to show the simulated parameters of the network. With this interface the Transit managers (or researchers) can analyze the simulated scenario and introduce new changes into the simulation boundary conditions.



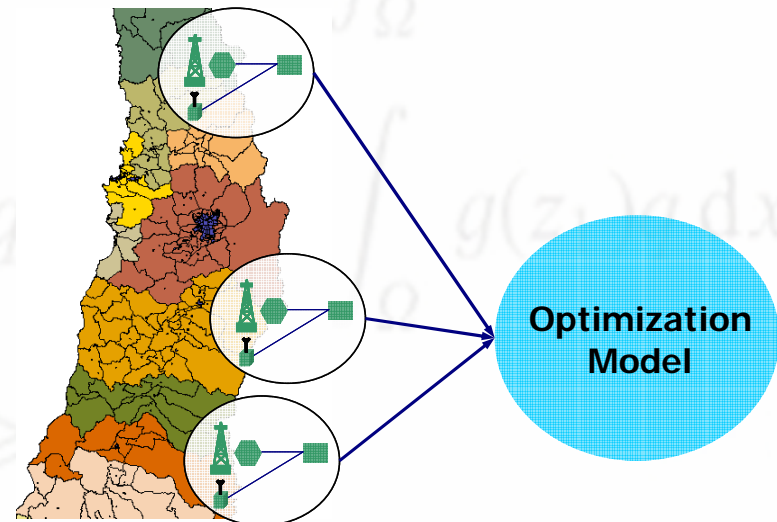
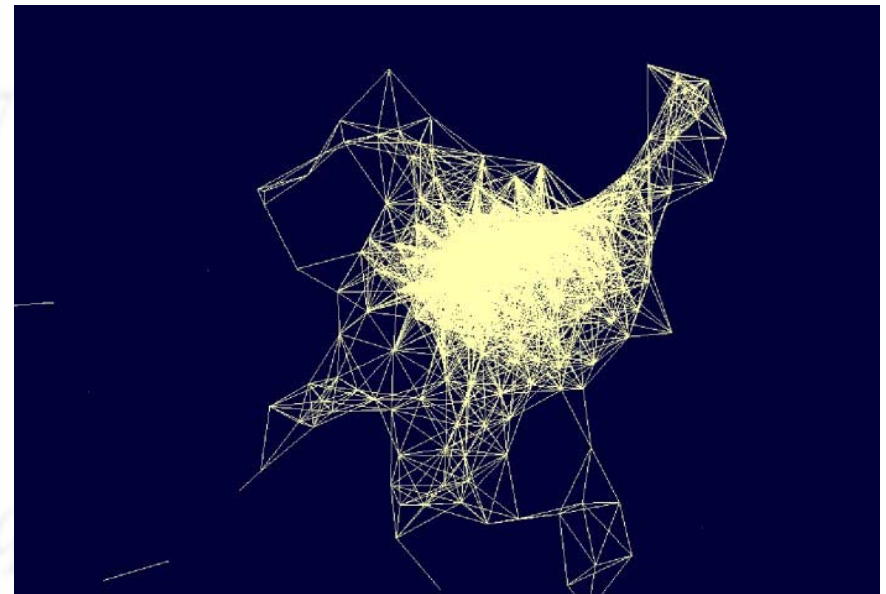


# Optimization and Equilibrium in the Telecommunications Market

We have generated new models, calculation algorithms and processes for implementation and validation of efficient business models that allow the setting of rates for the services provided by landline and mobile phone companies.

## Keywords

- ✓ Deregulated market models
- ✓ Mobile and fixed local phone systems
- ✓ Equilibrium/optimization problem and high performance computing





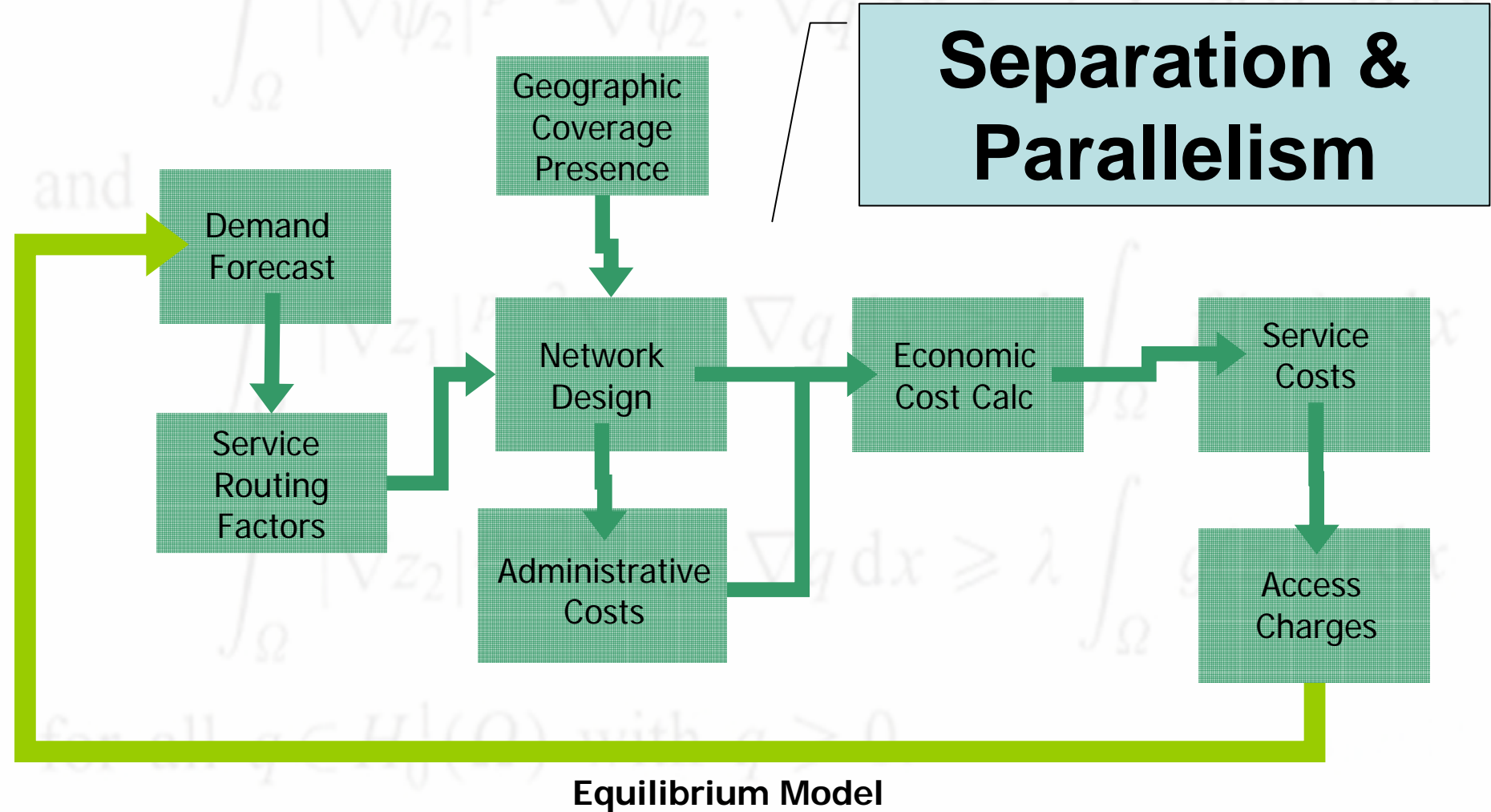
# Optimization and Equilibrium in the Telecommunications Market

- **Models:**

- LRIC (TSLRIC) cost model for Mobile and Fixed Telecommunication Networks
  - Chilean, Colombian and Peruvian Models
- Mobile Telecommunication Networks Expansion Planning and Localization of MSC Devices Model
- We also started to model and solve the problem of GSM BTS frequency assignment
- Market Equilibrium Model for Mobile Telecommunications on the Access Charge Segment

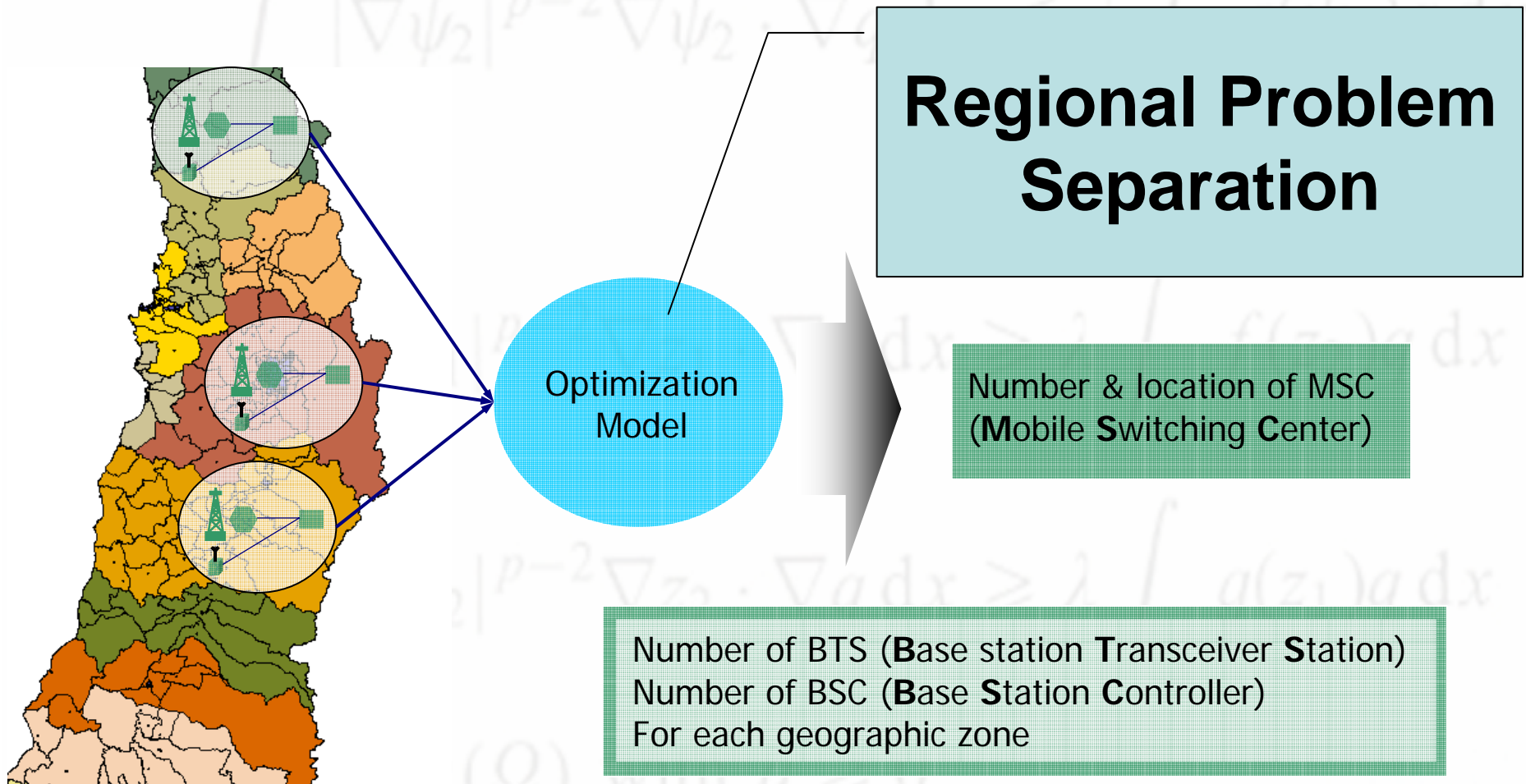
# Optimization and Equilibrium in the Telecommunications Market

## GENERAL MODEL FOR MOBILE ACCESS CHARGES



# Optimization and Equilibrium in the Telecommunications Market

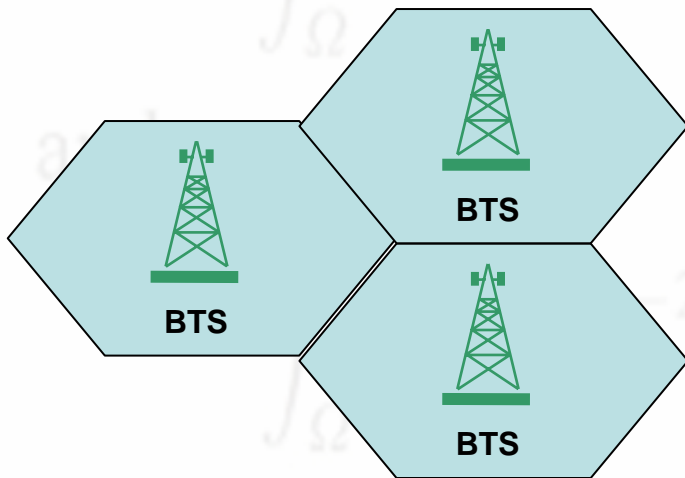
## GENERAL MODEL – MSC LOCALIZATION



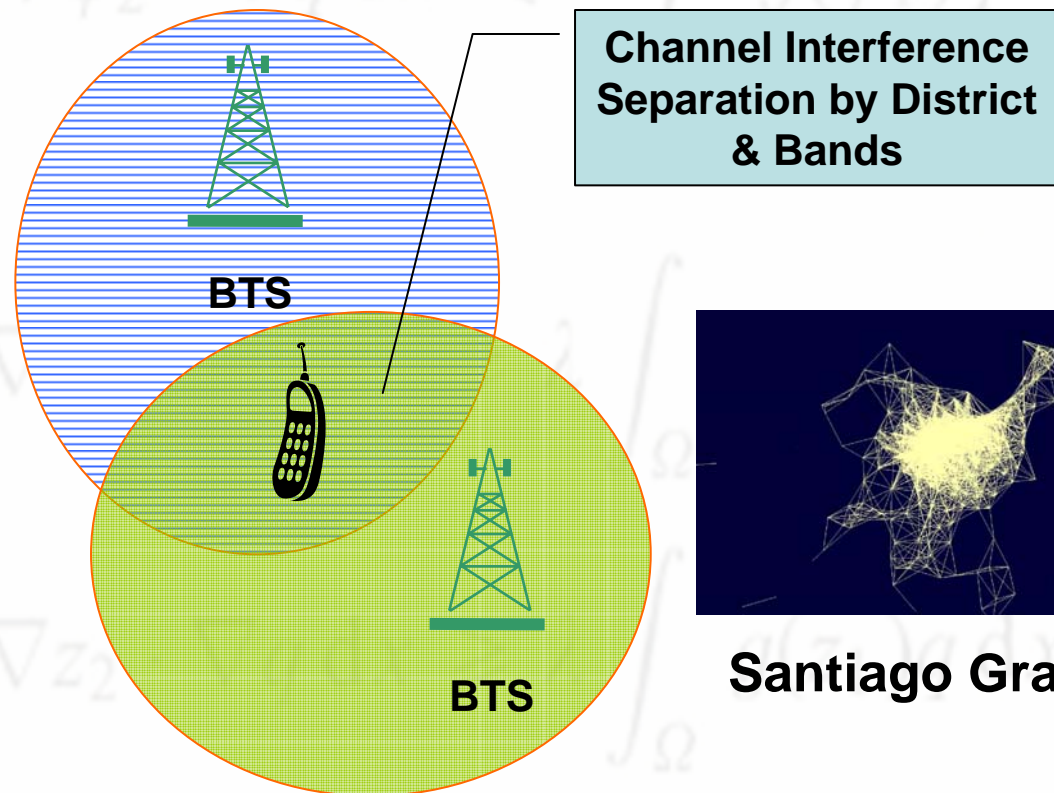


# Optimization and Equilibrium in the Telecommunications Market

## GENERAL MODEL – FREQUENCY ASSIGNMENT



**IDEAL CONFIGURATION**  
There is no Interference



**REAL CONFIGURATION**



**Santiago Graph**

# Optimization and Equilibrium in the Energy Market

We have created new models and improved some algorithms for coordinating the use of water reservoirs in hydrothermal energy systems. Especially using Stochastic Programming. We are also working on the problem of Optimal Expansion of Electrical Power Systems.

## Keywords

- ✓ Energy Markets Regulation
- ✓ Hydrothermal Coordination
- ✓ Equilibrium/optimization problem and high performance computing



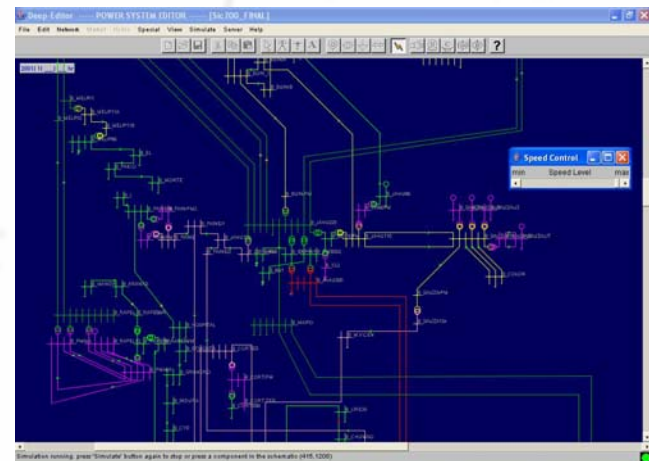
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# Optimization and Equilibrium in the Energy Market

## HYDROTHERMAL COORDINATION MODEL

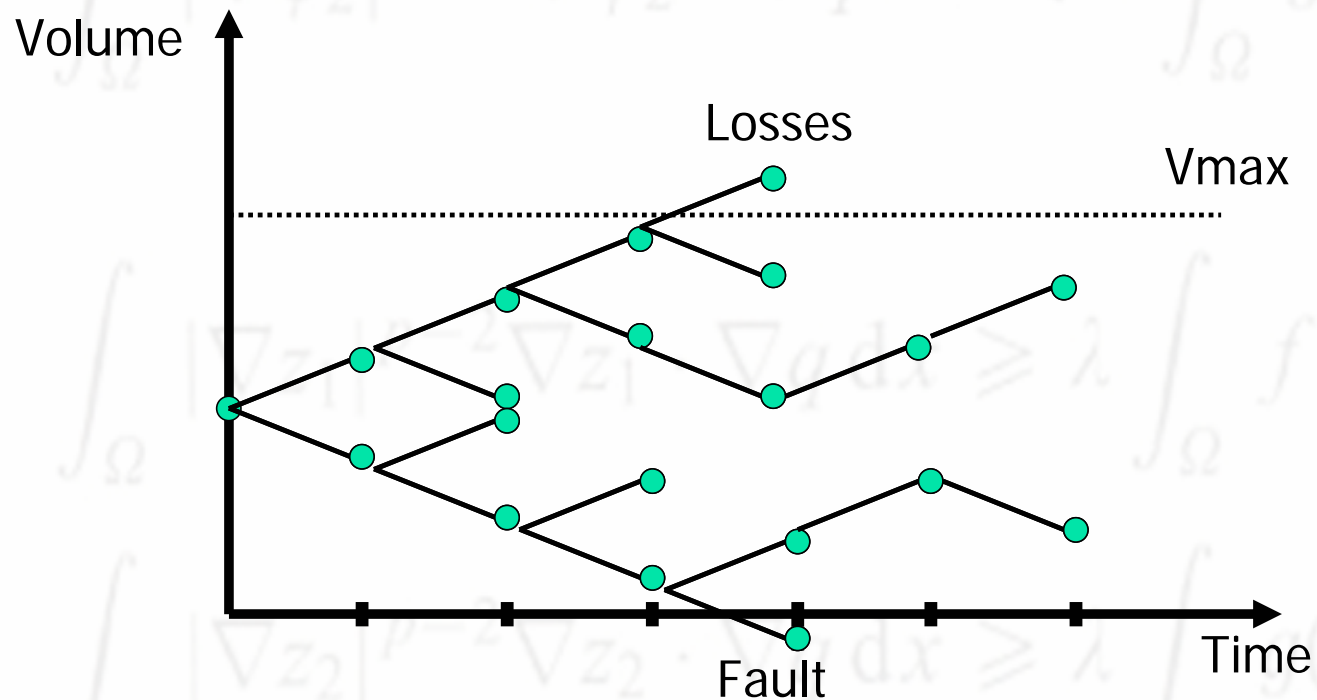
The main objective is to establish an appropriated policy of administration and use of the water reservoirs in an electrical power system





# Optimization and Equilibrium in the Energy Market

## HYDROTHERMAL COORDINATION MODEL

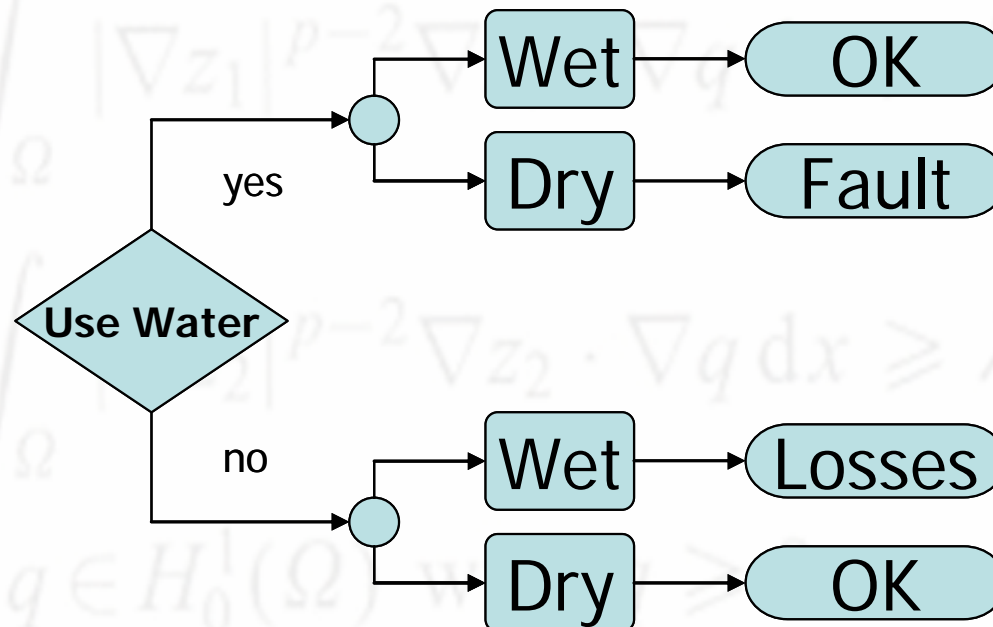


Separation on the Sampling Tree

# Optimization and Equilibrium in the Energy Market

## HYDROTHERMAL COORDINATION MODEL

- The problem of the high number of scenarios combinations is solved using an approximation which involves a sampling of the Scenarios Tree



# Optimization and Equilibrium in the Energy Market

## HYDROTHERMAL COORDINATION MODEL

- The main idea is to solve each scenario sequence as a separated problem, then we use it to turn this problem into a parallel problem

